7-modular lattices and a septic base Jacobi identity

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A quadratic Jacobi identity to the septic base is introduced and proved by means of modular lattices and codes over rings. As an application the theta series of all the 6-dimensional 7-modular lattices with an Hermitian structure over $\mathbb{Q}(\sqrt{-7})$ are derived.