Extreme value theory is gradually becoming part of standard statistical knowledge. The unifying approach that has been developed over the last decades has clearly indicated that both theory and practice of extreme value methodology have matured. We will survey the most important aspects of the theory. To illustrate the theoretical results we give a number of applications from insurance and geology.